

# Graph Condensation for Continual Graph Learning

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# Contents

- Continual Graph Learning
- Related Work
- CaT
- PUMA

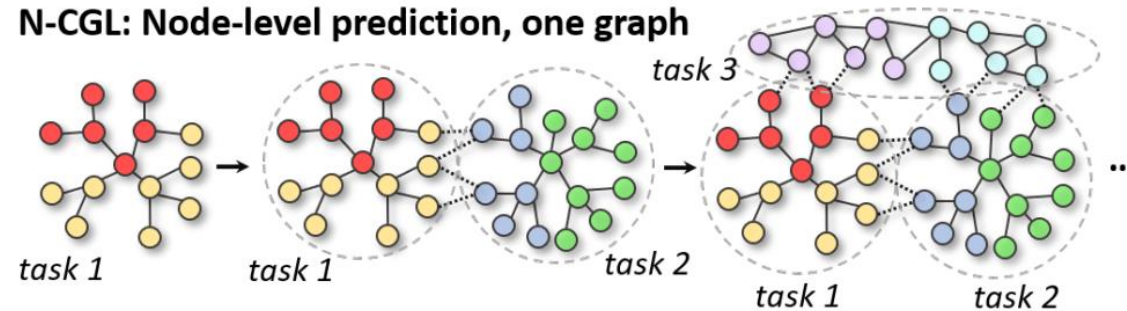
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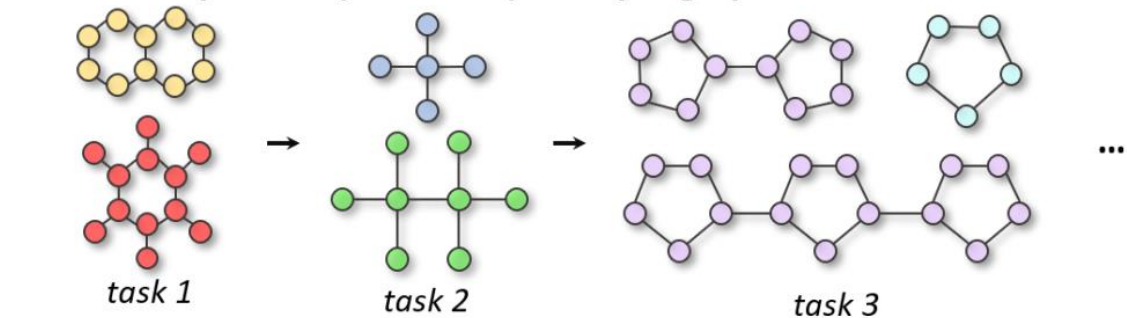
# Continual Graph Learning (CGL)

- Traditional Graph Neural Networks (GNNs) are not good at **streaming** inputs.
- **New** nodes can appear **dynamically**

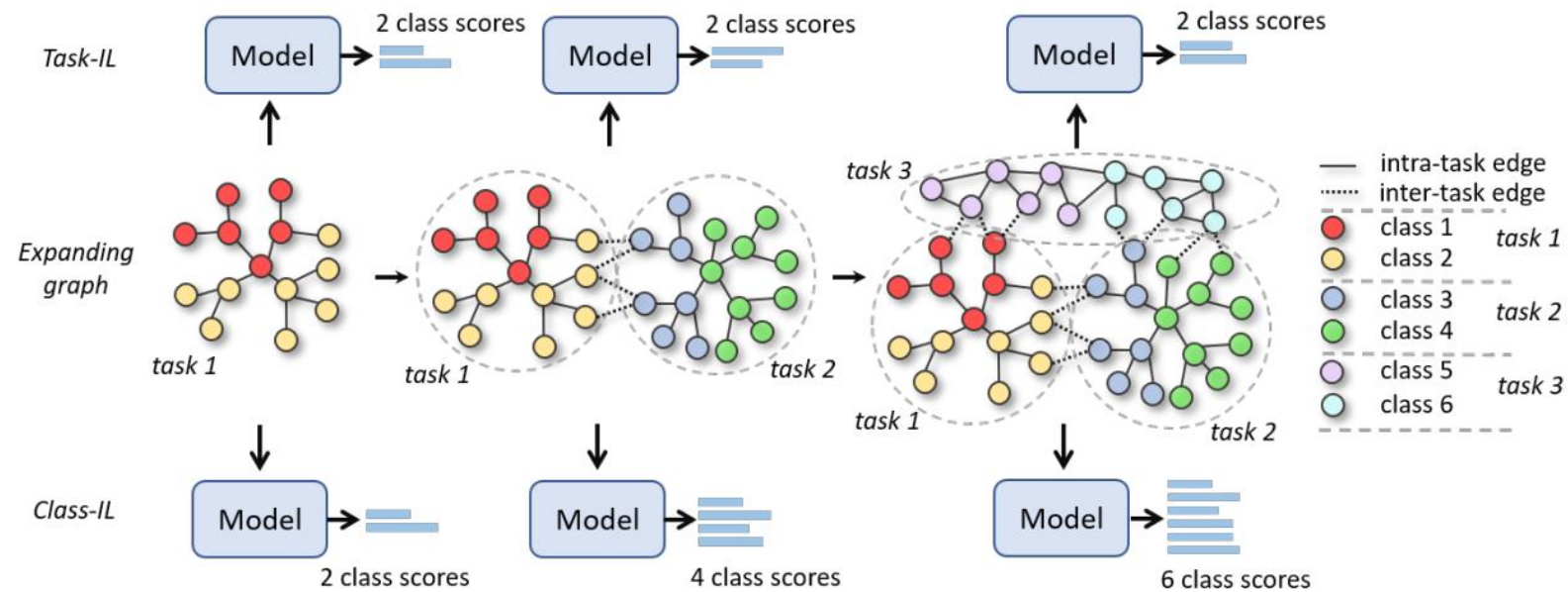
**N-CGL: Node-level prediction, one graph**



**G-CGL: Graph level prediction, multiple graphs**



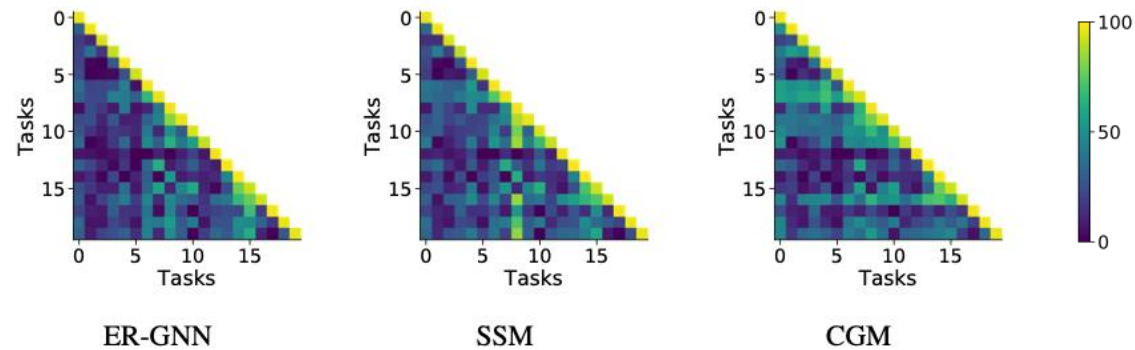
# Class/Task Incremental Learning (IL)



- **Class-IL** is much **harder** than Task-IL

# Catastrophic Forgetting (CF)

- CF is a **general** challenge in CGL
- **Old** knowledge covered by **new** ones.

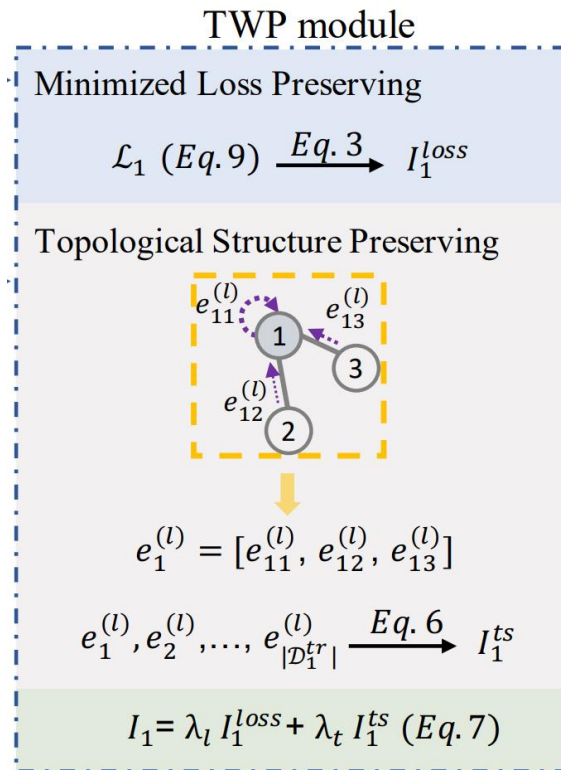


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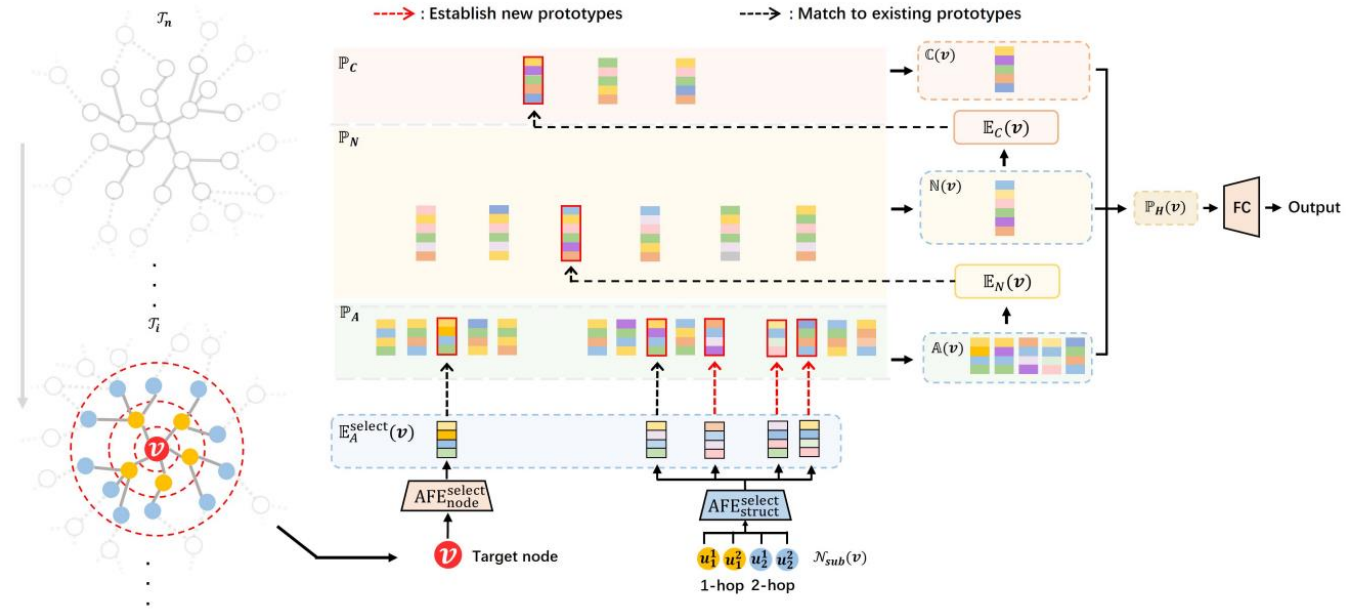
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# Related Work

- Regularisation-based: TWP



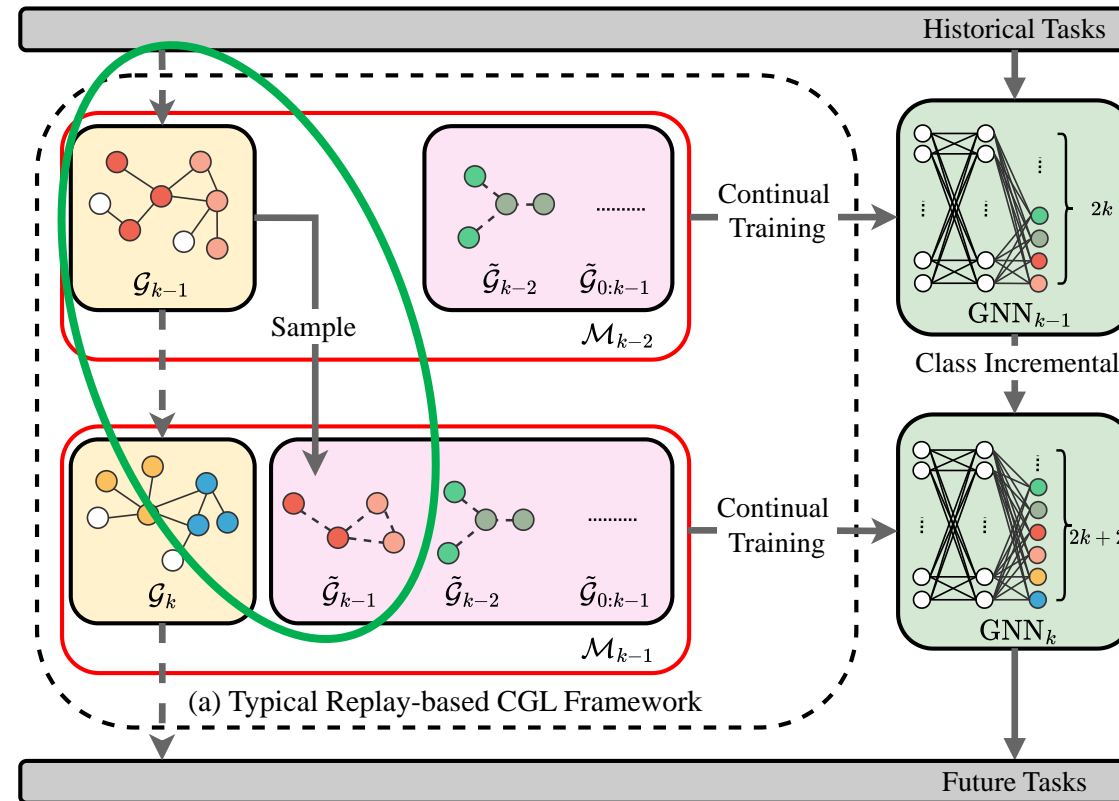
- Architecture-based: HPNs





# Related Work

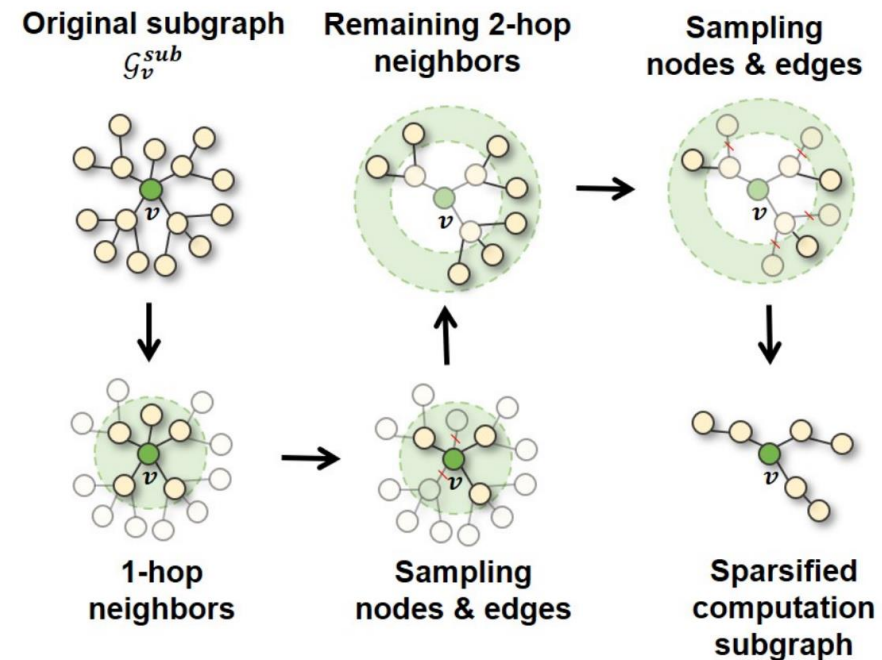
- Replay-based



# Related Work

- Replay-based: ER-GNN
  - Mean feature
  - Coverage Maximization
  - Influence Maximization

- SSM



# Contents

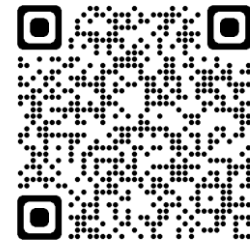
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# CaT 🐱 : Balanced Continual Graph Learning with Graph Condensation

Yilun Liu, Ruihong Qiu, Zi Huang

The University of Queensland

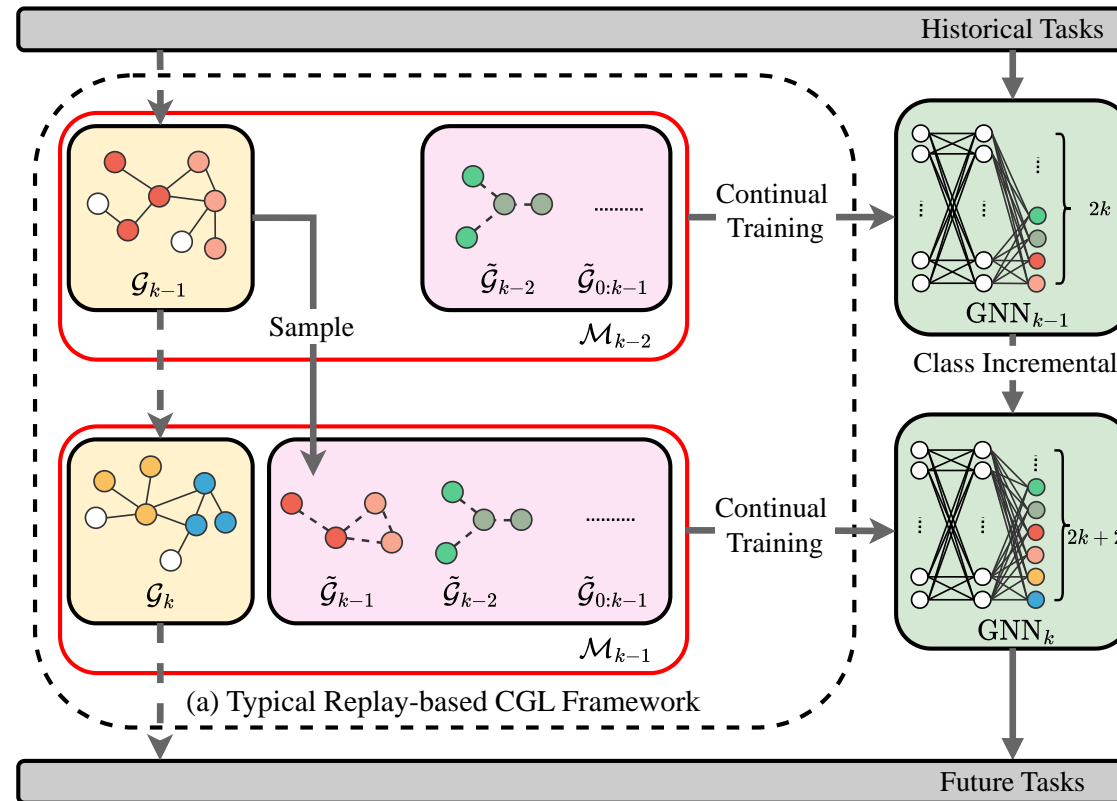
yilun.liu@uq.edu.au



<https://github.com/superallen13/CaT-CGL>

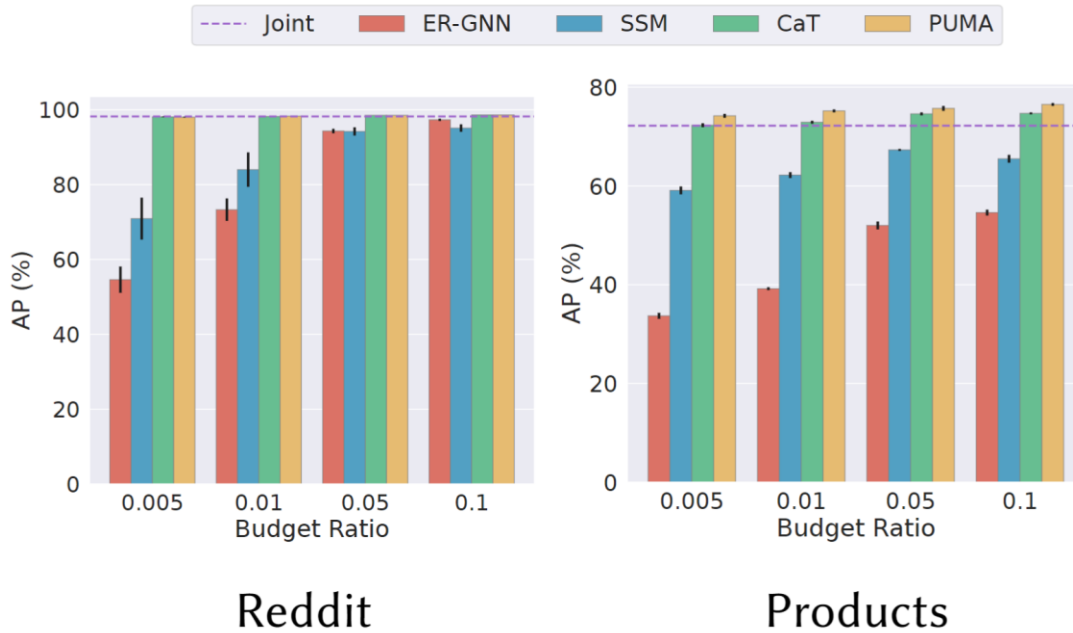
# Batch Training in Replay-based CGL

- Sample and combine

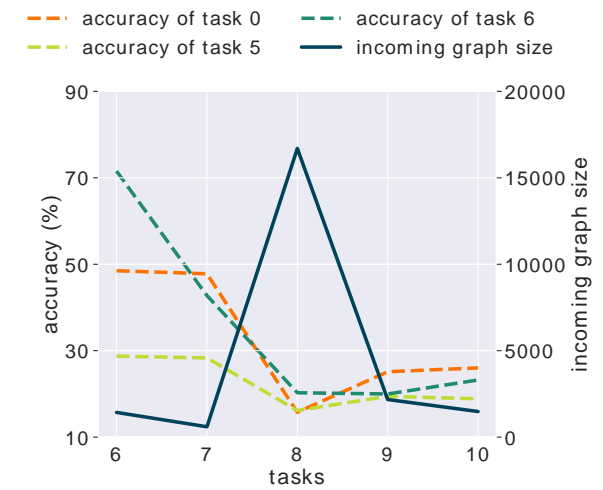
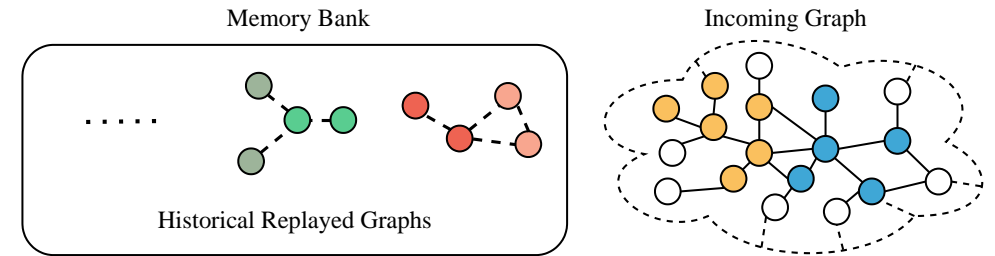


# Challenges in Replay

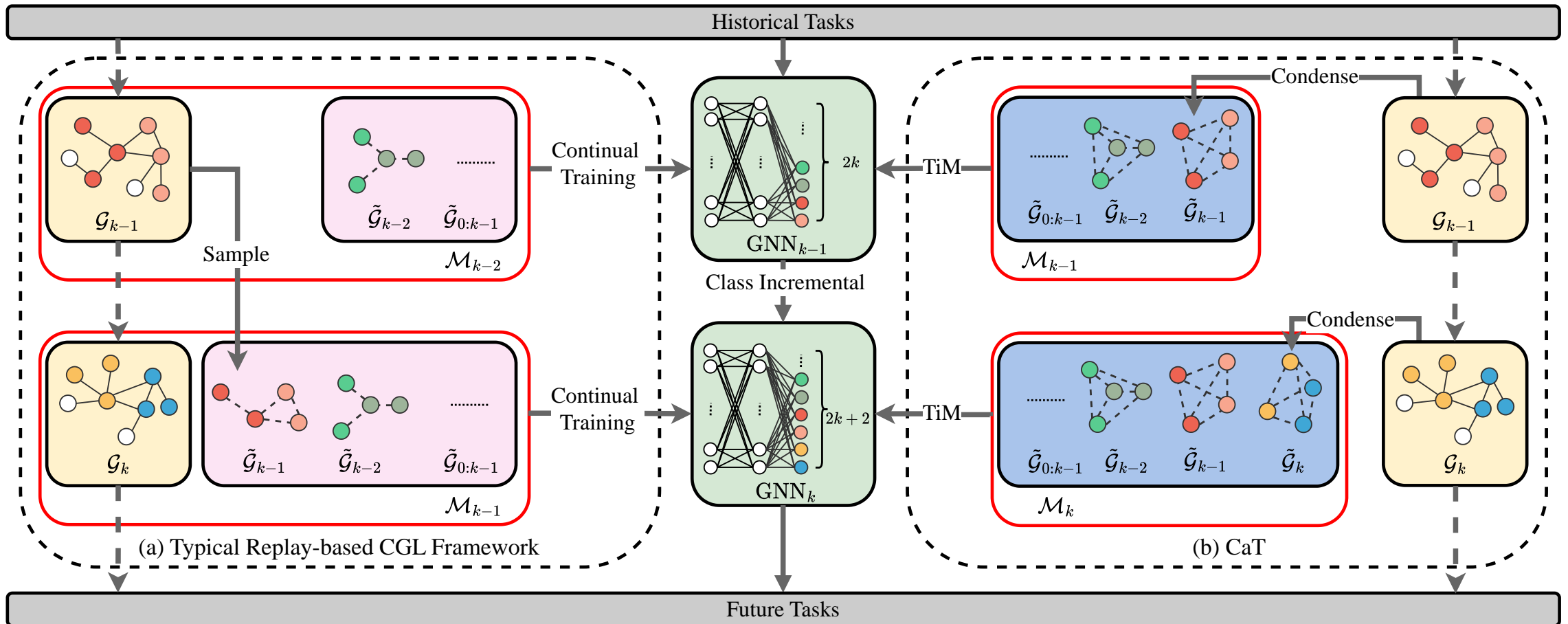
- **Large** storage requirement



- **Imbalanced** training graph size



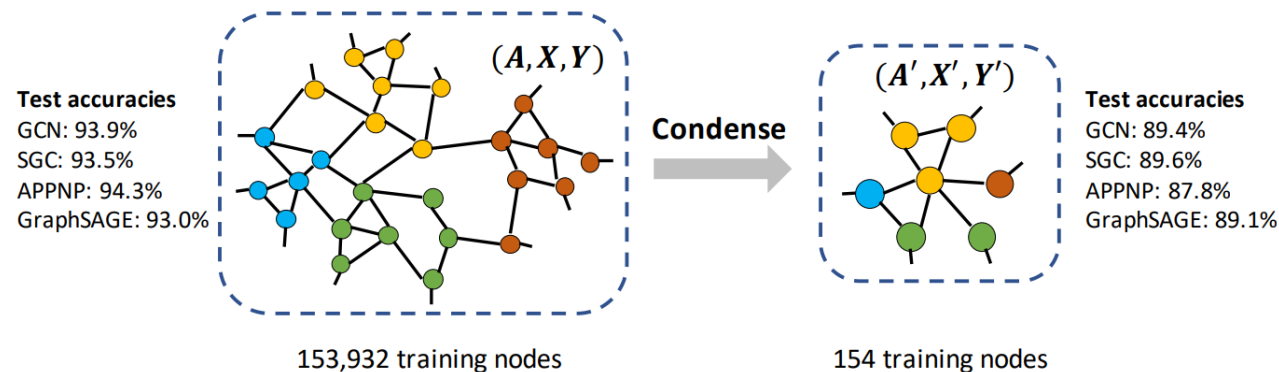
# Condense and Train (CaT) Framework



# Graph Condensation

- Smaller yet effective
- Model **performance** trained **on condensed** graph matches on **original** graph
- **Bi-level** optimisation problem

$$\min_{\tilde{G}} \mathcal{L}(G; \tilde{\theta}), s. t. \tilde{\theta} = \operatorname{argmin}_{\theta} \mathcal{L}(\tilde{G}; \theta)$$





# Condensed Graph Memory (CGM)

- **Distribution matching** method.
- **Random** GNN encoder to obtain latent features.
- Minimise **MMD** losses

$$\ell_{\text{MMD}} = \sum_{c \in \mathcal{C}_k} r_c \cdot \|\text{Mean}(\mathbf{E}_{k,c}) - \text{Mean}(\tilde{\mathbf{E}}_{k,c})\|^2$$

# Train in Memory (TiM)

- Condense **incoming** graph
- **Balanced** replayed graphs.

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## Algorithm 2: Overall procedure of CaT

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**Input:** A streaming of tasks  $\{\mathcal{T}_1, \mathcal{T}_2, \dots, \mathcal{T}_K\}$

**Output:**  $\text{GNN}_K$

```

1 Initialise a CGL model  $\text{GNN}_0$ ;
2 Initialise an empty memory bank  $\mathcal{M}_0$ ;
3 for  $k \leftarrow 1$  to  $K$  do
4   | Extract incoming graph  $\mathcal{G}_k$  from  $\mathcal{T}_k$ ;
5   | Obtain  $\tilde{\mathcal{G}}_k$  by CGM; /* Algorithm 1 */
6   |  $\mathcal{M}_k = \mathcal{M}_{k-1} \cup \tilde{\mathcal{G}}_k$ ; /* Eq. 11 */
7   | Update  $\text{GNN}_{k-1}$  to  $\text{GNN}_k$ ; /* Eq. 12 */
8 end
  
```

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# Implementation

- Baselines
  - Joint: **full-size**.
  - ER-GNN: informative **nodes**.
  - SSM: **subgraphs**.
- Metrics
  - Average performance (AP):  $\frac{1}{k} \sum_{i=1}^k m_{k,i}$
  - Backward transfer (BWT):  $\frac{1}{k-1} \sum_{i=1}^{k-1} m_{k,i} - m_{i,i}$

- Experiment settings
  - Dataset splitting [CGLB, NeurIPS 2022]
    - Each task contains two classes.
  - Task incremental learning (task-IL)
    - Classification heads are growing.

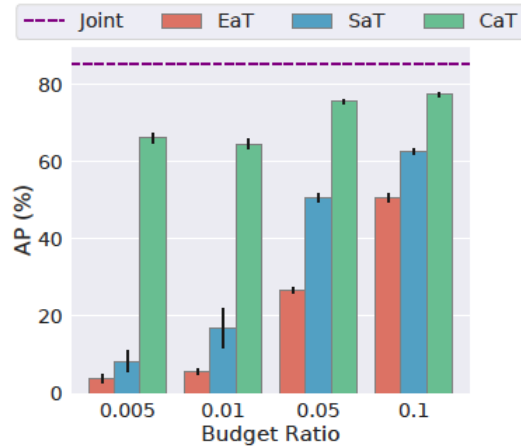
Dataset	Nodes	Edges	Features	Classes	Tasks
CoraFull	19,793	130,622	8,710	70	35
Arxiv	169,343	1,166,243	128	40	20
Reddit	227,853	114,615,892	602	40	20
Products	2,449,028	61,859,036	100	46	23

# Overall Results

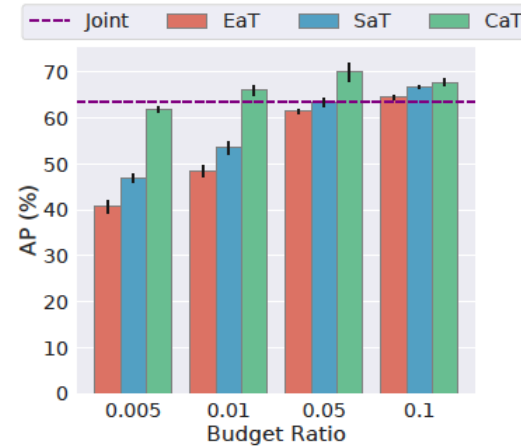
Category	Methods	CoraFull		Arxiv		Reddit		Products	
		AP (%) ↑	BWT (%) ↑	AP (%) ↑	BWT (%) ↑	AP (%) ↑	BWT (%) ↑	AP (%) ↑	BWT (%) ↑
Lower bound	Finetuning	2.2±0.0	-96.6±0.1	5.0±0.0	-96.7±0.1	5.0±0.0	-99.6±0.0	4.3±0.0	-97.2±0.1
Regularisation	EWC	2.9±0.2	-96.1±0.3	5.0±0.0	-96.8±0.1	5.3±0.6	-99.2±0.7	7.6±1.1	-91.7±1.4
	MAS	2.2±0.0	-94.1±0.6	4.9±0.0	-95.0±0.7	10.7±1.4	-92.7±1.5	10.1±0.6	-89.0±0.5
	GEM	2.5±0.1	-96.6±0.1	5.0±0.0	-96.8±0.1	5.3±0.5	-99.3±0.5	4.3±0.1	-96.8±0.1
	TWP	<u>21.2±3.2</u>	<u>-67.4±1.6</u>	4.3±1.1	-93.0±8.3	9.5±2.0	-35.5±5.5	6.8±3.5	-64.3±12.8
Distillation	LWF	2.2±0.0	-96.6±0.1	5.0±0.0	-96.8±0.1	5.0±0.0	-99.5±0.0	4.3±0.0	-96.8±0.2
Replay	ER-GNN	4.0±0.7	-94.3±0.9	30.8±0.6	-68.3±0.7	31.8±4.0	-71.2±4.2	39.5±1.3	-48.2±1.4
	SSM	16.2±2.8	-82.1±2.9	<u>35.1±1.8</u>	<u>-63.7±1.9</u>	<u>51.6±6.4</u>	<u>-50.3±6.7</u>	<u>62.7±0.5</u>	<u>-22.1±0.5</u>
Full dataset	Joint	85.3±0.1	-2.7±0.0	63.5±0.3	-15.7±0.4	98.2±0.0	-0.5±0.0	72.2±0.4	-5.3±0.5
Ours	CaT	<b>64.5±1.4</b>	<b>-3.3±2.6</b>	<b>66.0±1.1</b>	<b>-13.1±1.0</b>	<b>97.6±0.1</b>	<b>-0.2±0.2</b>	<b>71.0±0.2</b>	<b>-4.8±0.4</b>

- **Replayed**-based methods are overall **better**.
- **CaT** is the **best**, sometimes can **match** the ideal **Joint** scenario.

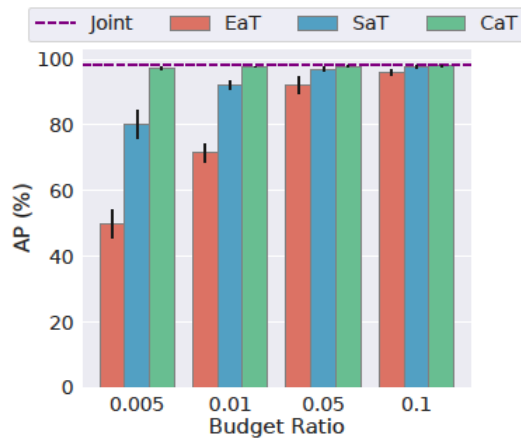
# Effectiveness of CGM



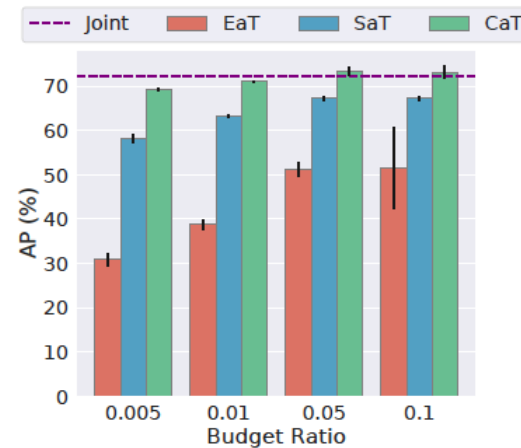
(a) CoraFull



(b) Arxiv



(c) Reddit

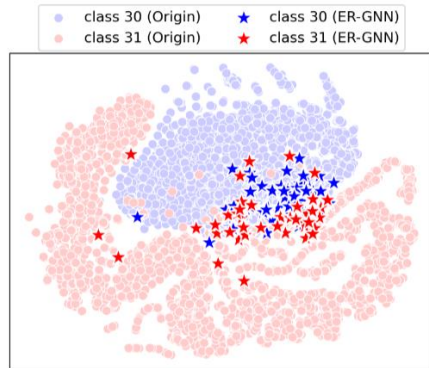


(d) Products

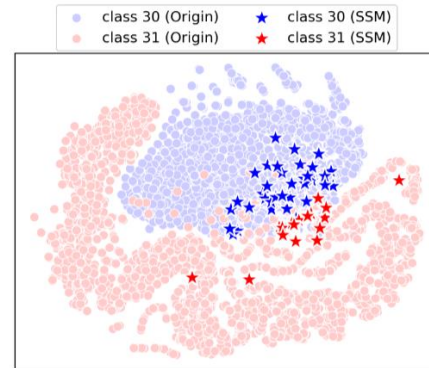
- Use TiM for ER-GNN and SSM
- **CGM** is **more effective** than other memory banks

# Visualisation of CGM

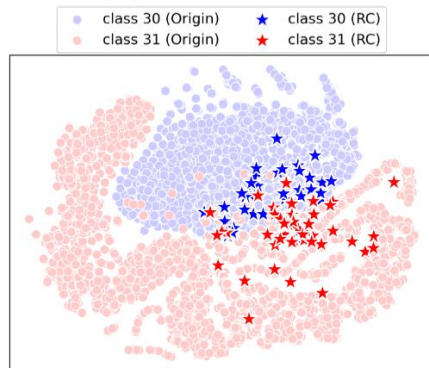
- Good **coverage** of the **original** distribution



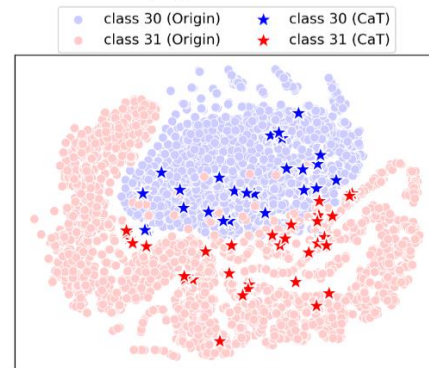
(a) ER-GNN



(b) SSM

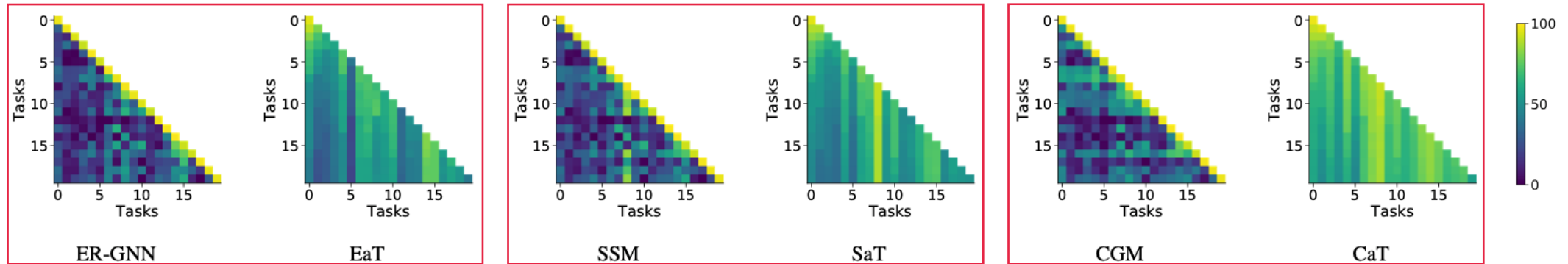


(c) Random Choice



(d) CGM

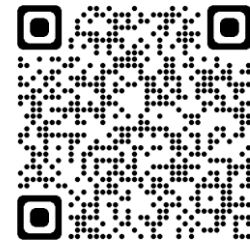
# TiM for Catastrophic Forgetting



- TiM has a **balanced** learning to **solve CF**.

# Conclusion

1. **CGM**: Graph **condensation** gives a **small** yet **effective** memory bank
2. **TiM**: A training scheme for **balanced** continual learning



<https://github.com/superallen13/CaT-CGL>



# Contents

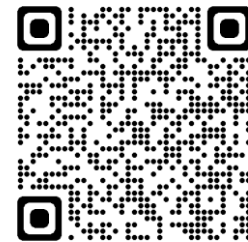
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- PUMA

# PUMA 🐯 : Efficient Continual Graph Learning via Retraining with Pseudo-label Guided Graph Condensation

Yilun Liu, Ruihong Qiu, Yanran Tang, Zi Huang

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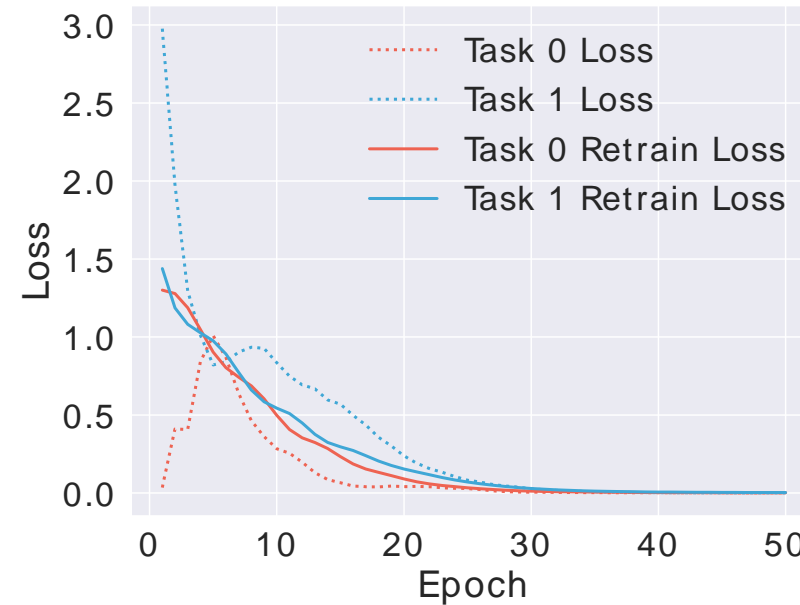
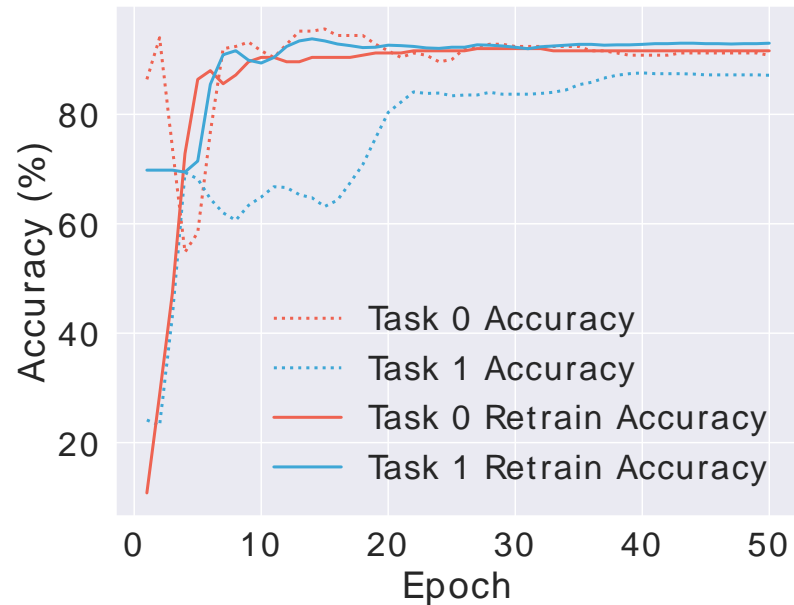


<https://github.com/superallen13/PUMA>

# Problems of CaT

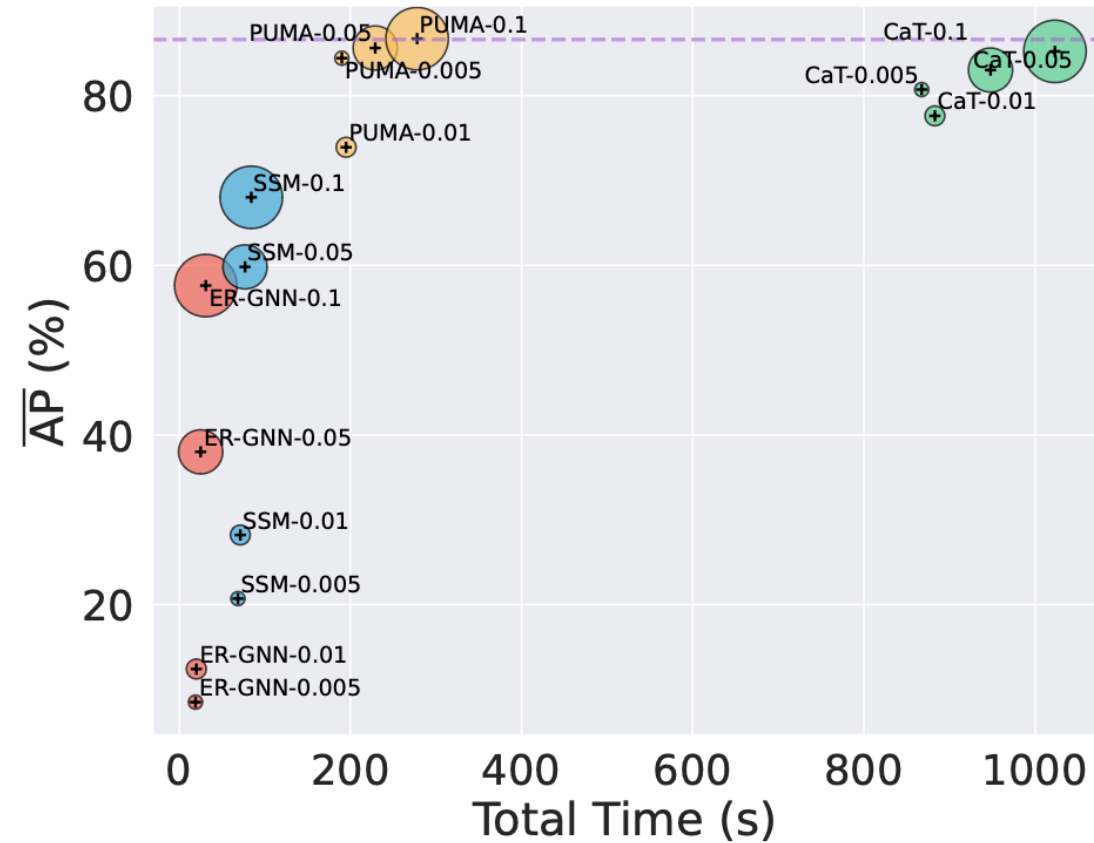
1. **Unlabelled** nodes in streaming graph data

2. **Still imbalance** historical knowledge

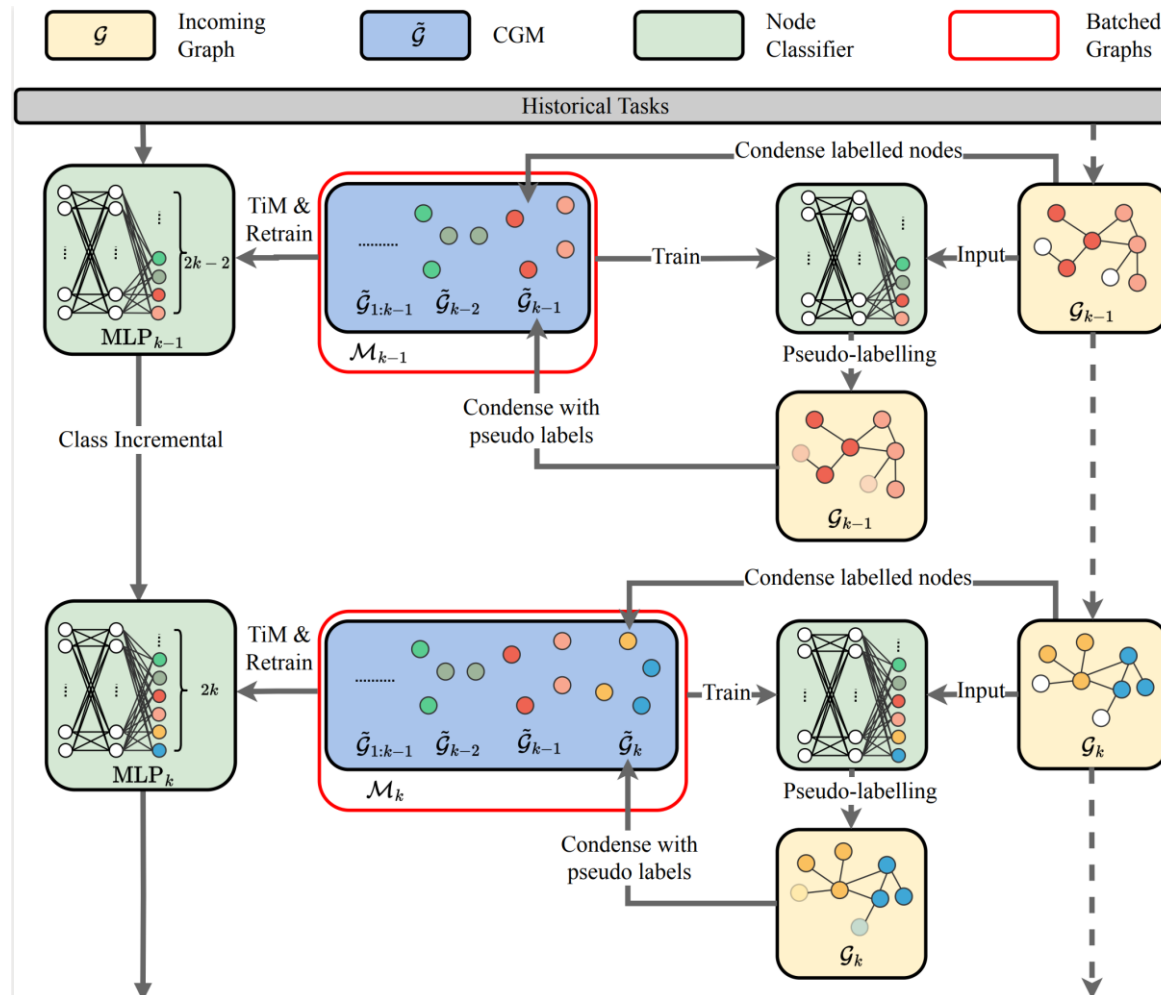


# Problems of CaT

## 3. **Slow** condensation and training



# PUMA Framework



# Pseudo Labelling-Guided CGM

- An extra classifier for **pseudo labels**
- Select unlabelled nodes with a **high** confidence score
- **Condense both labelled** and confidently **pseudo labelled** nodes

# Train from Scratch

- **No** more **continual** training, but retraining **from scratch**
- **Balanced** historical knowledge and incoming knowledge.

# Fast Condensation and Training

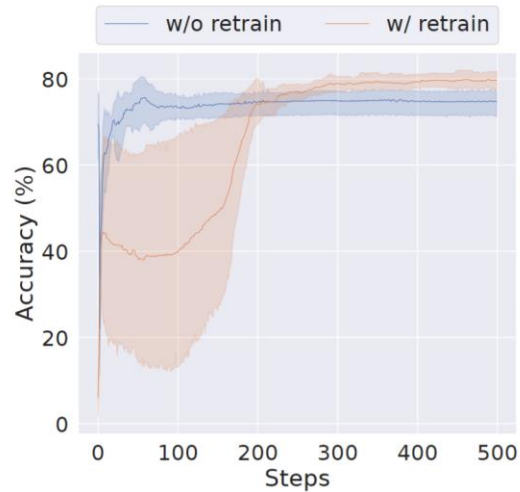
- One-time propagation
- Wide graph encoders
- They are fast in calculation and not sacrificing performance. Details in paper



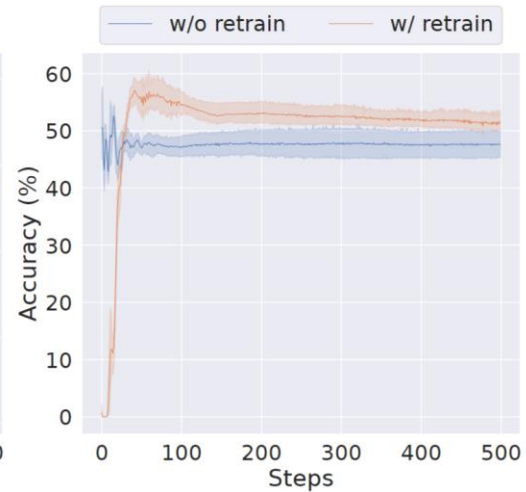
# Overall Performance

Category	Methods	CoraFull		Arxiv		Reddit		Products	
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	GEM	2.5±0.1	-96.6±0.1	5.0±0.0	-96.8±0.1	5.3±0.5	-99.3±0.5	4.3±0.1	-96.8±0.1
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Replay	ER-GNN	3.1±0.2	-94.6±0.2	23.2±0.5	-77.1±0.5	20.0±3.0	-83.7±3.1	34.0±1.0	-55.7±0.8
	SSM	3.5±0.5	-94.7±0.5	26.4±0.8	-73.7±0.9	41.8±3.2	-60.8±3.4	58.1±0.4	-29.3±0.5
Full dataset	Joint	85.3±0.1	-2.7±0.0	63.5±0.3	-15.7±0.4	98.2±0.0	-0.5±0.0	72.2±0.4	-5.3±0.5
Condensation	CaT (ours)	<u>68.5±0.9</u>	<u>-5.7±1.3</u>	<u>64.9±0.3</u>	<u>-12.5±0.8</u>	<u>97.7±0.1</u>	<u>-0.4±0.1</u>	<u>71.1±0.3</u>	<u>-5.4±0.3</u>
	PUMA (ours)	<b>77.9±0.2</b>	<b>-4.2±0.9</b>	<b>67.0±0.1</b>	<b>-12.2±0.3</b>	<b>98.0±0.1</b>	<b>-0.3±0.1</b>	<b>74.2±0.4</b>	<b>-4.1±0.5</b>

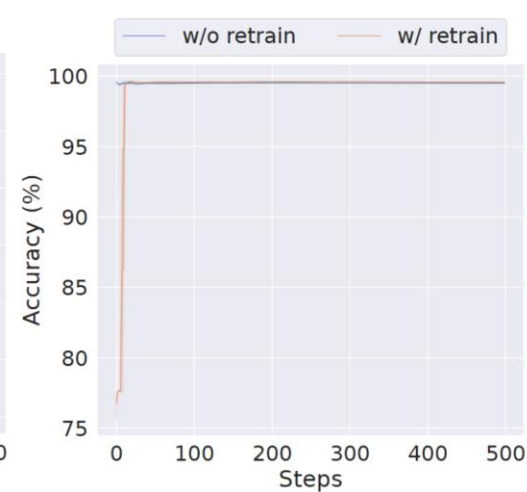
# Effectiveness of Retraining



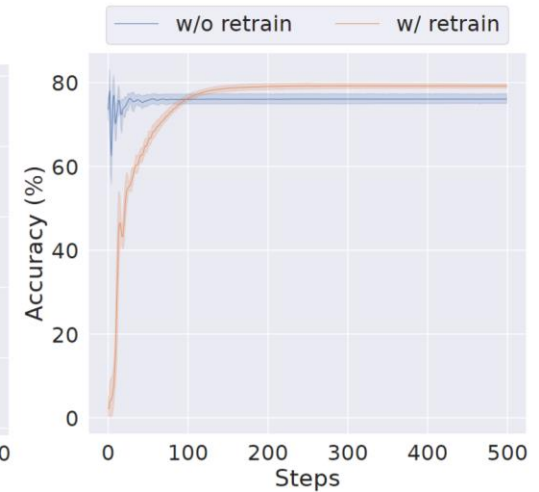
(a) CoraFull



(b) Arxiv



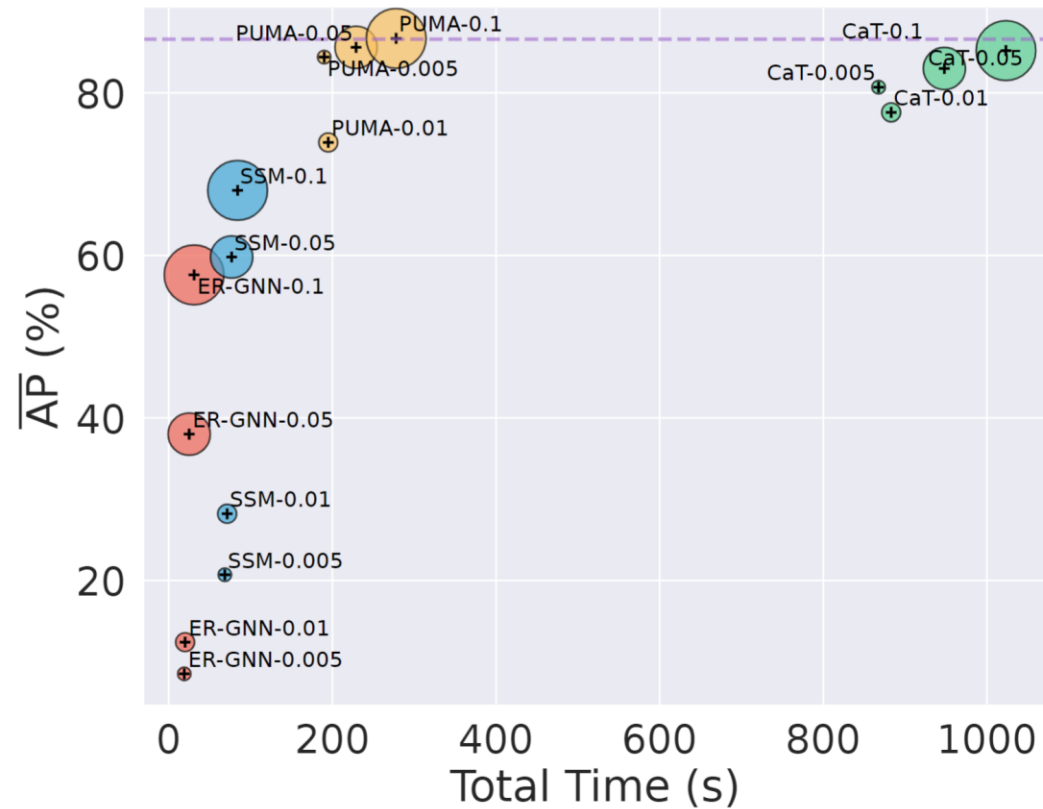
(c) Reddit



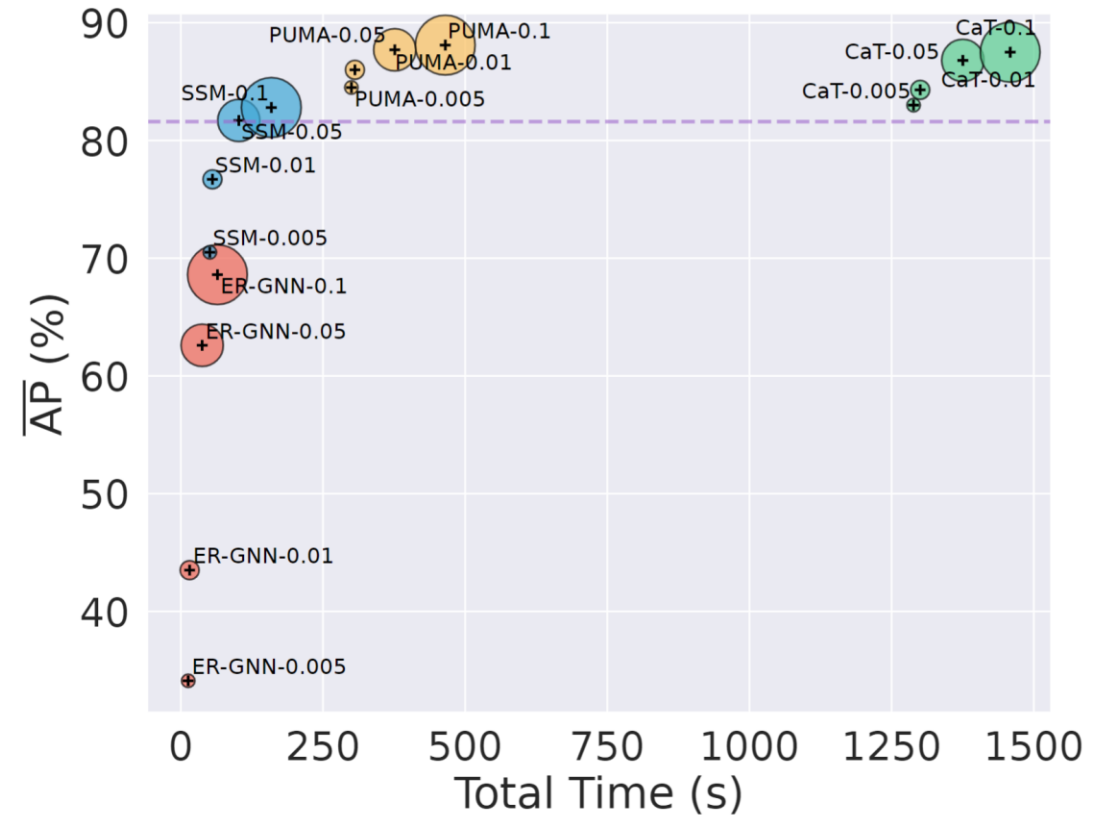
(d) Products

- **Converge higher**

# Time Efficiency



(a) CoraFull



(b) Products

- **PUMA is fast and performs well**

# Conclusion

1. **Unlabelled** nodes help with condensation
2. **Retraining** improve the performance
3. Careful designs to **accelerate**

# Q&A

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